

**ASME PTC 19.1-2013**  
(Revision of ASME PTC 19.1-2005)

# Test Uncertainty

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**Performance Test Codes**

**AN AMERICAN NATIONAL STANDARD**



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Mechanical Engineers**

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